

An Introduction to Self-Similar and Combinatorial Tiling Part 1

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Introduction

Tile: A set that is a closure of its interior.



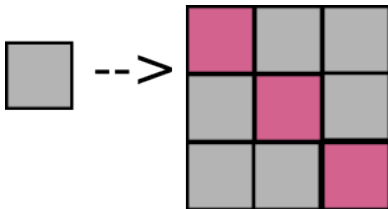
Example:

Patch: A finite union of tiles that do not intersect.

Example:

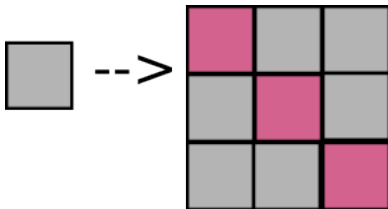


Inflate and Subdivide



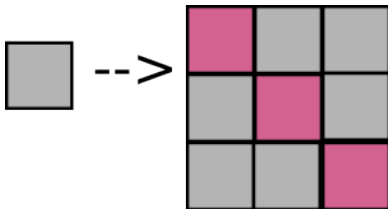
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- Inflate and Subdivide: Map a tile to a union of tiles.
- Inflates by using an expanding similarity of the plane.
- Subdivides by dividing the image into a union of the original tile.

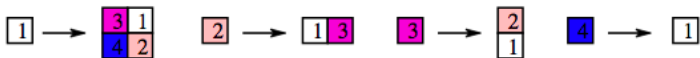
In this example, inflate and subdivide is present.

An Example of a Substitution Rule

- Substitution rule: Rule used to construct infinite tiling using a finite number of tiles.

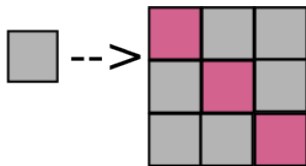
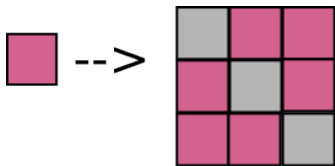
An Example of a Substitution Rule

- Substitution rule: Rule used to construct infinite tiling using a finite number of tiles.
- We will define a substitution to generate larger patches. Our rule is:



- This is a combinatorial substitution and it does not have a single expanding similarity.

Inflate and Subdivide and Substitution Rule



This example is both a substitution rule and inflate and subdivide rule.

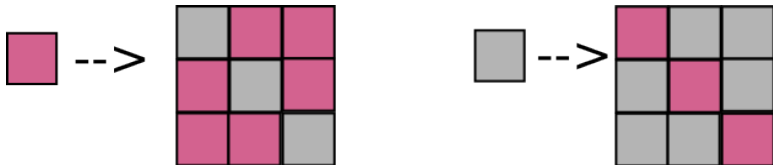
Self-Similar Tiling

- Self-similar tiling substitution: Substituted with a linear expansion of itself.

Self-Similar Tiling

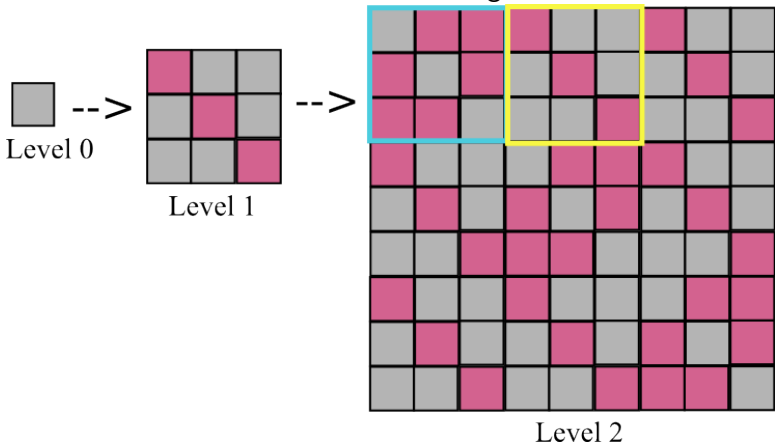
- Self-similar tiling substitution: Substituted with a linear expansion of itself.
- There is only one linear expansion for each substitution.

Example:

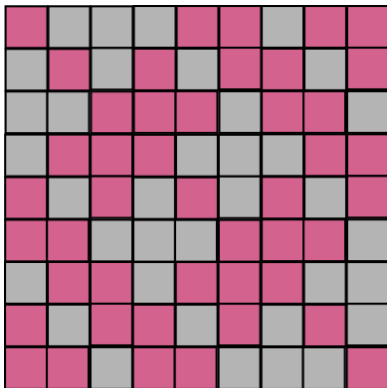


Create Level- n Patches

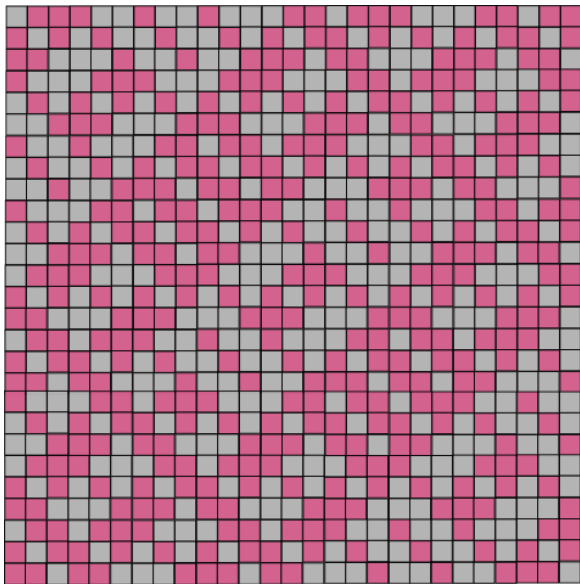
Level- n tiles: The level after substituting n times.



Self-Similar Tiling Activity

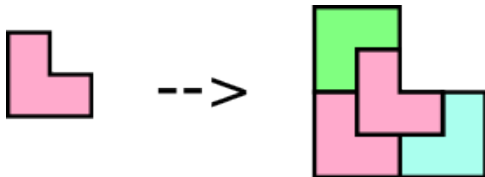


Self-Similar Tiling Activity



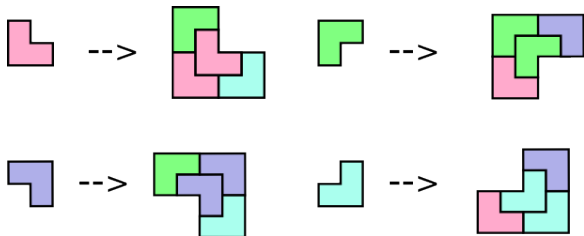
Chair Tiling: Inflate and Subdivide

The chair tiling has inflate and subdivide present.



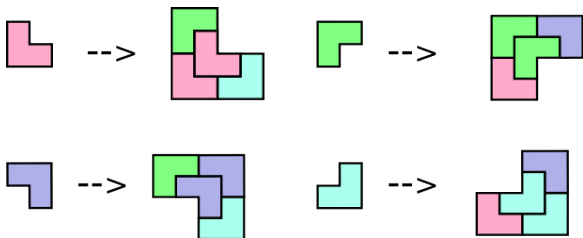
Chair Tiling: Substitution Rule

We will use inflate and subdivide to create a substitution rule to produce the chair tiling. The substitution rule for the chair tiling is:

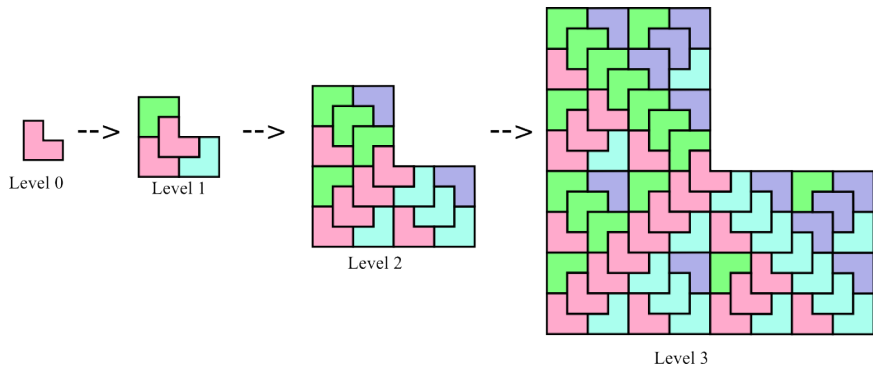


Chair Tiling: Self-Similar Tiling

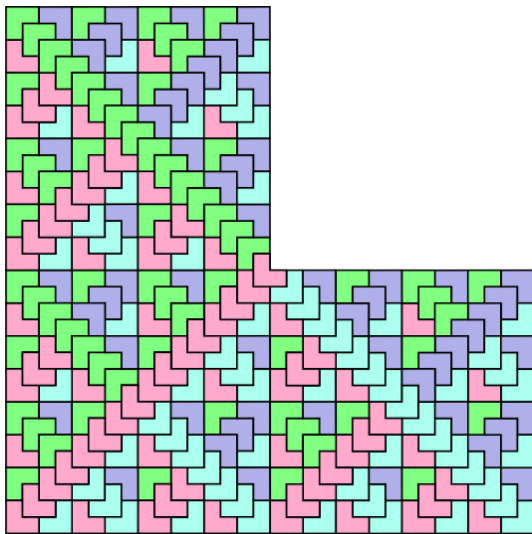
The chair tiling is a more advanced self-similar tiling.



Self-Similar Tiling: Chair Tiling Activity



Self-Similar Tiling: Chair Tiling Level 4



Level 4

Conclusion

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- Combinatorial tiling substitution: Substitution rule that replaces a tile by some arrangement of tiles.
- Does not have a geometric resemblance to the original tile.
- Does not keep the constant length of the original tile.

Conclusion

- This leads into our second talk which is on combinatorial tiling.
- Combinatorial tiling substitution: Substitution rule that replaces a tile by some arrangement of tiles.
- Does not have a geometric resemblance to the original tile.
- Does not keep the constant length of the original tile.
- Our second talk will be presented by Moises Rivera.

References

- For more information on self-similar tiling:

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