

## HW #7 - due Tuesday, 11/15 in class

Kutner Ch. 10:

## Problem 1

Kutner Ch. 11:

## Question 2 – research beyond the text is encouraged

## Problems: 1, 7

Plus these:

1. Consider a  $1M_{\odot}$  **neutron star** with a radius of 15 km, rotating 100 times per second.
  - a) Calculate the gravitational acceleration,  $g$ , at the surface.
  - b) Calculate the centripetal acceleration at the equator, and compare with  $g$ .
  - c) How fast (in rotations per second) would the neutron star have to be rotating for the two accelerations to be equal? What do you think would happen then? (Then see #3, below for the white dwarf story.)
  
2. The **tidal force** is a differential force  $-dF/dr$ : the difference between the force at one distance and the force at another. If  $dr$  happens to correspond to, say, your height, then the tidal force is the difference in gravity felt by your head and by your feet. This amounts to a stretching force, since one end is pulled harder than the other end. Calculate the tidal force experienced by your body at the surface of a neutron star. Assume that the neutron star has a mass of  $1.5 M_{\odot}$  and a radius of 10 km. Assume that your mass is 100 kg. and that your  $dr$  (height) is 2 m when standing and 0.5 m when prone.
  - a) What is the tidal force when you are standing?
  - b) What is the tidal force when you are prone?
  - c) Based on the above, what do you recommend for minimizing the tidal force?
  - d) Compare the tidal **acceleration** you feel at the surface of that neutron star with what you feel at the surface of the earth., i.e., divide your answer in part a by  $g_{\oplus}$ ; how many “g’s” do you feel on the neutron star? (You might be interested to know that the maximum limit for the human body, for a very brief duration, is  $100 g_{\oplus}$ .)
  
3. If a star rotates too rapidly, it will break apart. One way to think about this is to say that, in order to remain bound, the rotational speed of a particle on the surface of a star must be less than the circular orbital speed at that radius.
  - a) For a star of mass  $M$ , and radius  $R$ , write down the expressions for the rotational speed of a particle on the star’s equator, and for the circular orbital speed. Now equate these speeds and solve for  $P^2$ . Where have we seen this equation before?
  - b) Consider a **white dwarf** of mass  $1 M_{\odot}$  and  $R=10^4$  km. What is the value of  $P$  you get from the equation in part a? This represents the *minimum possible period* that the white dwarf can have; if it rotated any faster, it would break up. How many rotations per second does this correspond to?
  - c) Could rotating white dwarfs explain all pulsars? If not, what else might you suggest?