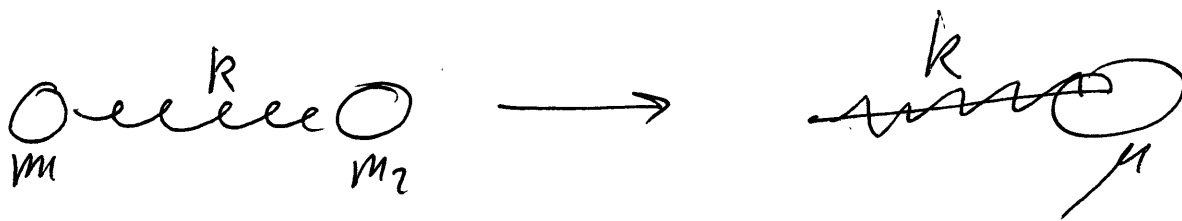


# HARMONIC OSCILLATOR



$$\mu = \frac{m_1 m_2}{m_1 + m_2}$$

$$V(x) = \frac{1}{2} k x^2$$

$$\hat{H} = -\frac{\hbar^2}{2\mu} \frac{d^2}{dx^2} + \frac{1}{2} k x^2$$

$$\hat{H} \psi_n = -\frac{\hbar^2}{2\mu} \frac{d^2 \psi_n}{dx^2} + V(x) \psi_n$$

$$= E_n \psi_n$$

$$\psi_n(x) = A_n e^{-\alpha x^2/2} H_n(\sqrt{\alpha} x)$$

$$E_n = \hbar \sqrt{\frac{k}{\mu}} \left( \frac{1}{2} + n \right) = \hbar \nu \left( \frac{1}{2} + n \right)$$

$n = 0, 1, 2, \dots$

$$\nu = \frac{1}{2\pi} \sqrt{\frac{k}{\mu}}$$

$$\langle \hat{V} \rangle = ?$$

$$\langle \hat{K} \rangle = ?$$

$$\Delta x \Delta p \doteq ?$$

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$$-\frac{\hbar^2}{2\mu} \frac{1}{R_0} \frac{d^2 \Phi}{d\phi^2} = E \Phi$$

$$\Phi \sim \mathcal{O}^{\pm im\phi}$$

BC

$$\mathcal{O}^{\pm im\phi} = \mathcal{O}^{\pm im(\phi + 2\pi)}$$

$$\Rightarrow \mathcal{O}^{\pm i2\pi m} = 1$$

$$\cos(2\pi m) \pm i \sin(2\pi m) = 1$$

$$2\pi m \Rightarrow m \in \mathbb{N}$$

$$m = 0, \pm 1, \pm 2, \pm 3, \dots$$

$$E_m = \frac{\hbar^2}{2\mu R_0^2} m^2 = \frac{\hbar^2}{2I} m^2 \quad m=0, \pm 1, \dots$$

$$I = \mu R_0^2$$

$$\Phi_m(\phi) = \frac{1}{\sqrt{2\pi}} e^{im\phi}$$

## Review 18.7 Rigid Rotor