

ENERGY

KINETIC ENERGY

POTENTIAL ENERGY

$U \leftarrow$ INTERNAL ENERGY

$U \leftrightarrow$ vibrations, rotations, chemical bonds

FIRST LAW

$$\Delta U_{\text{UNIVERSE}} = 0$$

$$\Delta U_{\text{SYS}} + \Delta U_{\text{SUR}} = 0$$

FOR SYSTEMS WITH NO CHEMICAL RXN
NO PHASE TRAN

$$\Delta U = q + W$$

$q = \text{heat}$

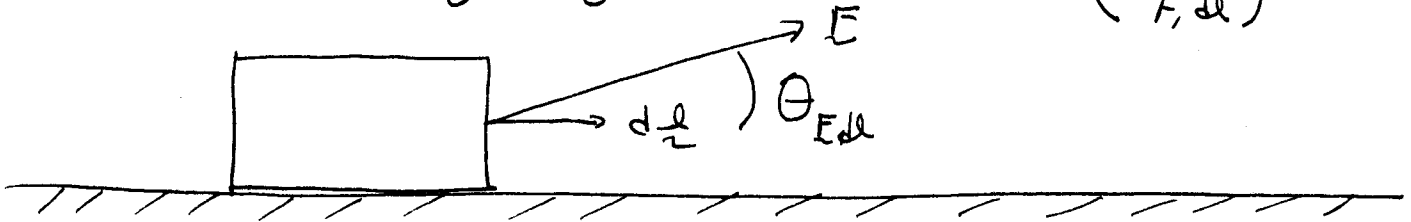
$W = \text{work}$

$q \equiv \text{heat} \equiv$ flow of energy across a boundary due to a temperature difference

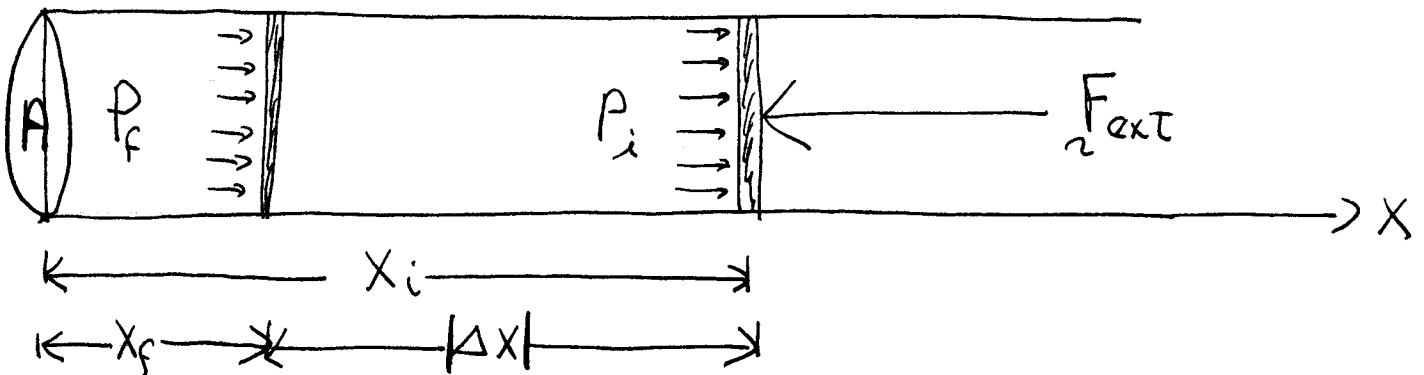
WORK

FROM CLASSICAL MECHANICS, WORK ON A SYSTEM BY A FORCE \vec{F} IS

$$dW \equiv \vec{F} \cdot d\vec{\ell} = |\vec{F}| |d\vec{\ell}| \cos(\theta_{F,d\ell})$$



LET US CONSIDER A GAS CONTAINED IN A CYLINDER BY A CONSTANT EXTERNAL FORCE.



IN A COMPRESSION \vec{F}_{ext} IS IN THE SAME DIRECTION AS Δx . THUS

$$\cos(\theta_{F,d\ell}) = \cos(0) = 1,$$

AND WE HAVE

$$\Delta W = |F_{ext}| |\Delta x|$$

BUT IN A COMPRESSION $\Delta X < 0$, THUS WE CAN WRITE

$$\Delta W = - |F_{\text{ext}}| \Delta X$$

SINCE $|\Delta X| = -\Delta X$.

IN AN EXPANSION, THE ANGLE BETWEEN \vec{F}_{ext} AND $d\vec{l}$ IS π , AND $\cos(\theta_{\vec{F}, d\vec{l}}) = -1$. MOREOVER, IN THIS CASE $\Delta X > 0$. THUS WE HAVE

$$\begin{aligned} \Delta W &= - |F_{\text{ext}}| |\Delta X| \\ &= - |F_{\text{ext}}| \Delta X. \end{aligned}$$

NOTICE THAT THE FORCE HAS TO CONSTRAIN THE GAS INTO THE PISTON. OTHERWISE, WE DO NOT HAVE A SYSTEM.

WE CAN SAY THAT \vec{F}_{ext} IS A POSITIVE IF CONSTRAINS THE GAS INTO THE CYLINDER AND NEGATIVE IF IT DOES NOT. IN THIS CASE, WE WILL NEVER HAVE A SYSTEM AT EQUILIBRIUM, NO MATTER HOW LONG WE WAIT.

IF WE CONSIDER THE AREA, A , OF THE PISTON

$$\Delta W = - \left(\frac{|F_{\text{ext}}|}{A} \right) A \Delta X.$$

BUT $|F_{\text{ext}}|/A = P_{\text{ext}}$ AND $A \Delta X = \Delta V = V_f - V_i$.
THE FINAL EXPRESSION FOR P-V WORK IS GIVEN BY

$$\Delta W = - P_{\text{ext}} \Delta V.$$

NOTICE THAT $\Delta W > 0$ ON A COMPRESSION ($V_f < V_i$)
AND $\Delta W < 0$ IN AN EXPANSION ($V_f > V_i$).

THE UNITS WILL BE

$$\text{atm} \cdot \text{L} = 1.013 \times 10^5 \text{ newton m}^{-2} (10^{-3} \text{ m}^3)$$

$$\text{atm} \cdot \text{L} = 101.3 \text{ newton m} = 101.3 \text{ J}$$

IF WE NOW CONSIDER INFINITESIMAL DISPLACEMENTS, WE GET AN EXPRESSION FOR INFINITESIMAL WORK

$$dW = - P_{\text{ext}} dV,$$

WHERE dW STANDS FOR AN INCOMPLETE DIFFERENTIAL.

HEAT (FORM OF ENERGY)

FOR A SYSTEM $q > 0 \Rightarrow \Delta T > 0$

$$q < 0 \Rightarrow \Delta T < 0$$

$$1 \text{ g H}_2\text{O} \leftrightarrow 1 \text{ cal} \Rightarrow \Delta T = 1^\circ\text{C}$$

$$1 \text{ cal} = 4.18 \text{ J g}^{-1} \text{ K}^{-1}$$

$$q \equiv C \Delta T$$

$$C = \frac{\Delta q}{\Delta T}$$

$$C = \frac{dq}{dT}$$

$$dq = C dT$$

$$q = \int_{T_i}^{T_f} C(T) dT$$

$C \rightarrow C_p$ CONSTANT P

C_v CONSTANT V

$$C_p = \lim_{\Delta T \rightarrow 0} \left(\frac{q_p}{\Delta T} \right)$$

$$C_v = \lim_{\Delta T \rightarrow 0} \left(\frac{q_v}{\Delta T} \right)$$

$$C_p > C_v$$

AT $P = \text{CONST}$ THE SYSTEM NEEDS TO DO WORK AND INCREASE ITS TEMPERATURE SO

$$q_p > q_v$$

FOR THE SAME FINAL TEMPERATURE.

ALTHOUGH

$$\Delta q \neq q_f - q_i = \int_i^f dq$$

AND

$$\Delta w \neq w_f - w_i = \int_i^f dw$$

THE COMBINATION

$$\begin{aligned}\Delta U &= \Delta q + \Delta w = U_f - U_i \\ &= \int_i^f dU\end{aligned}$$

REVERSIBLE PROCESS \Rightarrow THAT THE SYSTEM

AND ITS SURROUNDINGS ARE

IN THERMAL EQUILIBRIUM

\Leftrightarrow QUASI STATIONARY

STATE FUNCTION OR PATH INDEPENDENT FUNCTION

DEFINITION
IF ΔU DEPENDS ONLY ON THE INITIAL AND FINAL CONDITIONS, U IS A STATE FUNCTION

$$\Delta U = \int_i^f dU = U_f - U_i$$

COROLLARY $\Delta U = 0$ FOR A CLOSED PATH.

$$\Delta U = \oint dU = 0$$

WORK AND HEAT ARE NOT STATE FUNCTIONS

BUT

$$q + w = \Delta U$$

IS A STATE FUNCTION.