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Department of Mathematics and Statistics

**MATH 402 : MEASURE THEORY**

**Problem Set 3 – due Monday, October 5th**

**INSTRUCTIONS:**

You should aim to submit this assignment (via Glow) before Monday at **6pm**. Late assignments may be submitted by **3pm** on Tuesday; however, 5% will be deducted for submissions past Monday 6pm. Assignments will not be accepted after 3pm Tuesday under any circumstances. Please label your file in the format **Lastname-PS3**. If you're having difficulty scanning your work in a way that's legible, please let me or the TA know and we can try to help.

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**3.0** Read the textbook up through page 22.

**3.1** Prove that  $E \subseteq \mathbb{R}^n$  is measurable if and only if

$$m_*(S) = m_*(S \cap E) + m_*(S \cap E^c)$$

for every  $S \subseteq \mathbb{R}^n$ .

**3.2** Textbook exercises<sup>1</sup> 4, 5, 9, 11, 16, 20, 26, 29, 37

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<sup>1</sup>These are on pages 37–44; Exercises  $\neq$  Problems!