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## MATA32 – Calculus for Management I

### Problem Set 2 (due January 21, 2010)

**Read:** 4.1-4.2

**Problems:**

**Section 4.1** # 2, 4, 6, 13, 14, 16, 20, 22, 28

**Section 4.2** # 10, 12, 16, 18, 20, 22, 24, 30, 32, 36, 64

(a) Evaluate (to four digits of accuracy)  $\frac{\log_{10}(1+x)}{x}$  for  $x = 1, 0.1, 0.01, 0.001, 0.0001$ , and  $0.00001$ . Without calculating it, guess the value (to four digits of accuracy) of this function when  $x = 0.00000000000001$ .

(b) Evaluate  $\frac{\log_2(1+x)}{x}$  for  $x = 1, 0.1, 0.01, 0.001, 0.0001, 0.00001$ . Without calculating it, guess the value (to four digits of accuracy) when  $x = 0.00000000000001$ .

(c) Evaluate  $\frac{\log_3(1+x)}{x}$  for  $x = 1, 0.1, 0.01, 0.001, 0.0001, 0.00001$ . Without calculating it, guess the value (to four digits of accuracy) when  $x = 0.00000000000001$ .

(d) Approximate which base of the logarithm we would have to use for a function of the above form to tend to 1 as  $x$  gets closer and closer to 0. In other words, find a number  $b$  (accurate to three digits after the decimal point) such that  $\frac{\log_b(1+x)}{x} = 1.00$  for  $x = 0.00000000000001$ .