
Exercise 6

These computational exercises should be completed by **January 18** at **11:59AM**. Solutions should be turned in through the course website.

1. Advanced Plotting

Same as last time—although if you are interested in Matlab, enter `demo` at the prompt!

2. Random Walks

Use Mathematica (or your favorite language) to study the behavior of random walkers (in one or two dimensions). Here are a few things to try (

- Write a function that moves the walkers a variable number of steps using `Module`. Have the walkers' positions, step-size, and number of steps as variables for the function.
- Explore how the walk depends on the step-size, the number of walkers, and the number of steps.
- For the two-dimensional case, force each walker to move a fixed distance but in a random direction.
- Visualize the results using one of the visualization techniques such as `ListDensityPlot` and/or `ListAnimate` (it should look like the solution to the diffusion equation).

3. Partial Differential Equations

Use Mathematica to visualize the behavior of another partial differential equation. Here are some examples:

Diffusion with a Source:

$$\frac{\partial \rho}{\partial t} = D \frac{\partial^2 \rho}{\partial x^2} + f(x, t), \quad (1)$$

(try $f(x, t) = e^{-x^2} \sin \omega t$).

Reaction-Diffusion Equation ($\rho_1(x, t), \rho_2(x, t)$):

$$\frac{\partial \rho_1}{\partial t} = D_1 \frac{\partial^2 \rho_1}{\partial x^2} - \gamma_{12}(\rho_1 - \rho_2) \quad (2)$$

$$\frac{\partial \rho_2}{\partial t} = D_2 \frac{\partial^2 \rho_2}{\partial x^2} - \gamma_{12}(\rho_2 - \rho_1) \quad (3)$$

$$(4)$$

The Schrödinger Equation ($\Psi(x, t)$):

$$i\hbar \frac{\partial \Psi}{\partial t} = -\frac{\hbar^2}{2m} \frac{\partial^2 \Psi}{\partial x^2} + V(x, t)\Psi. \quad (5)$$

Wave Equation with a Source ($\Psi(x, t)$):

$$\frac{\partial^2 \Psi}{\partial t^2} = \frac{\partial^2 \Psi}{\partial x^2} + f(x, t). \quad (6)$$

Feel free to try two-dimensional versions, with $\partial^2 \Psi / \partial x^2 \rightarrow \partial^2 \Psi / \partial x^2 + \partial^2 \Psi / \partial y^2$.